

ASYMPTOTIC EXPANSION FOR LAYER SOLUTIONS  
OF A  
SINGULARLY PERTURBED REACTION-DIFFUSION  
SYSTEM

XIAO-BIAO LIN

ABSTRACT. For a singularly perturbed system of reaction-diffusion equations, assuming that the 0th order solutions in regular and singular regions are all stable, we construct matched asymptotic expansions for formal solutions to any desired order in  $\epsilon$ . The formal solution shows that there is an invariant manifold of wave-front-like solutions that attracts other nearby solutions. With an additional assumption on the sign of the wave speed, the wave-front-like solutions converge slowly to stable stationary solutions on that manifold.

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*Date:* March 8, 1994.

Research partially supported by NSF grant DMS9002803 and DMS9205535.

DEPARTMENT OF MATHEMATICS, NORTH CAROLINA STATE UNIVERSITY, RALEIGH,  
NORTH CAROLINA 27695-8205

*E-mail address:* `xblin@xblsun.math.ncsu.edu`